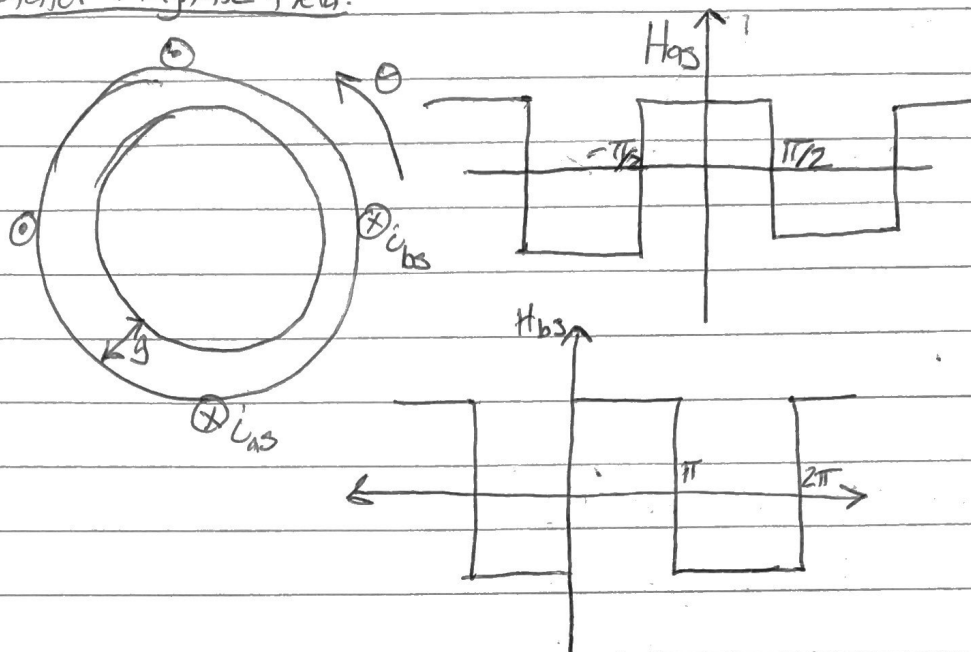


Correction for 2 phase
Stator Magnetic field:



$$H_{as} \approx \frac{N_s i_{as}}{2g} \cos(\theta)$$

$$H_{bs} \approx \frac{N_s i_{bs}}{2g} \sin(\theta)$$

Assume: $i_{as} = I_s \cos(\omega_s t)$
 ~~$i_{as} = I_s \cos(\omega_s t)$~~

$$i_{bs} = I_s \sin(\omega_s t)$$

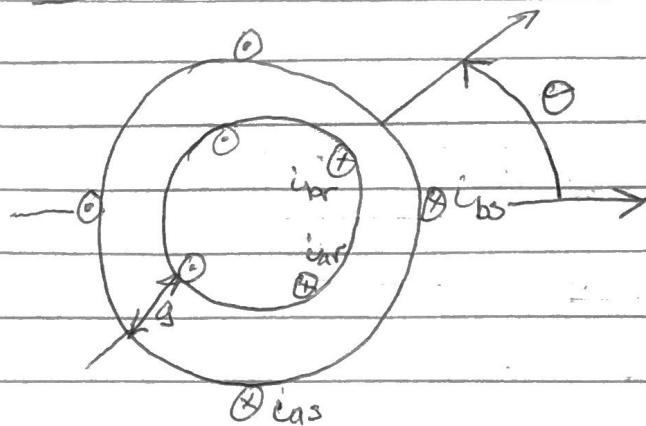
$$\begin{aligned} H_s &\approx H_{as} + H_{bs} \\ &= \frac{N_s I_s}{2g} (\cos(\omega_s t) \cos(\theta) + \sin(\omega_s t) \sin(\theta)) \end{aligned}$$

$$H_s = \frac{N_s I_s}{2g} \cos(\omega_s t - \theta)$$

$$t=0, \text{ max } H_s \text{ at } \theta=0$$

$$t=\tau, \text{ max } H_s \text{ at } \theta=\omega_s \tau$$

Two Phase Rotor-Stator



$$\begin{bmatrix} \lambda_{as} \\ \lambda_{bs} \\ \lambda_{ar} \\ \lambda_{br} \end{bmatrix} = \begin{bmatrix} L_s & 0 & M \cos(\theta) & -M \sin(\theta) \\ 0 & L_s & M \sin(\theta) & M \cos(\theta) \\ M \cos(\theta) & M \sin(\theta) & L_r & 0 \\ -M \sin(\theta) & M \cos(\theta) & 0 & L_r \end{bmatrix} \begin{bmatrix} i_{as} \\ i_{bs} \\ i_{ar} \\ i_{br} \end{bmatrix}$$

$$W_m' = \frac{1}{2} [L_s(i_{as}^2 + i_{bs}^2) + L_r(i_{ar}^2 + i_{br}^2)] + M \cos(\theta) i_{as} i_{ar} + M \sin(\theta) i_{bs} i_{ar} - M \sin(\theta) i_{as} i_{br} + M \cos(\theta) i_{bs} i_{br}$$

$$T_e = \frac{\partial W_m'}{\partial \theta} = -M \sin(\theta) [i_{as} i_{ar} + i_{bs} i_{br}] - M \cos(\theta) [i_{as} i_{br} - i_{bs} i_{ar}]$$

Assume: $i_{as} = I_s \cos(\omega_s t)$ $i_{ar} = I_r \cos(\omega_r t)$
 $i_{bs} = I_s \sin(\omega_s t)$ $i_{br} = I_r \sin(\omega_r t)$
 $\theta = \omega_m t + \gamma$

$$\Rightarrow T_e = -M I_s I_r \sin[(\omega_m - \omega_s + \omega_r)t + \gamma]$$

Frequency condition: $\omega_m = \omega_s - \omega_r$

* Gives constant torque

$$T_e = -M I_s I_r \sin(\gamma)$$

$$P = -\omega_m M I_s I_r \sin(\gamma)$$